

## Forecasting (Review)

1. Here are the least squares estimates from the fit to model  $\text{Price} = \beta_0 + \beta_1 \text{Size} + \varepsilon$ , where price is measured in units of \$1000 and size is measured in units of 100 ft<sup>2</sup>, along with the result of using the model to predict the mean price at size 2000 ft<sup>2</sup>.

The regression equation is  
price = 182 + 45.0 size

	Coef	SE Coef	T	P
Constant	182.27	62.43	2.92	0.010
size	44.95	4.37	10.29	0.000

S = 101.4    R-Sq = 86.9%    R-Sq(adj) = 86%

Predicted Values for New Observations

NewObs	Fit	SE Fit	95% CI	95% PI
1	1081.3	38.1	(1000.4, 1162.1)	(851.7, 1310.9)

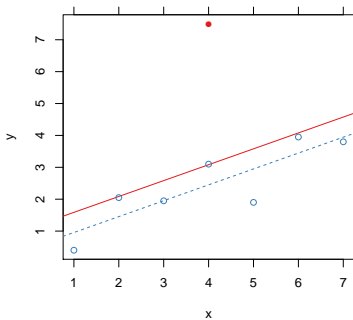
Values of Predictors for New Observations

NewObs	size
1	20.0

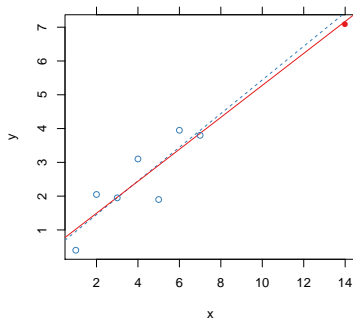
- (a) Find a 95% confidence interval for the mean price of all apartments with size 2000 ft<sup>2</sup>.
- (b) Find a 95% prediction interval for the price of a particular apartments with size 2000 ft<sup>2</sup>.
- (c) Make a statement about the prices of 95% of all apartments with size 2000 ft<sup>2</sup>.
- (d) What is the difference between the confidence interval and the prediction interval?

## Extreme Points

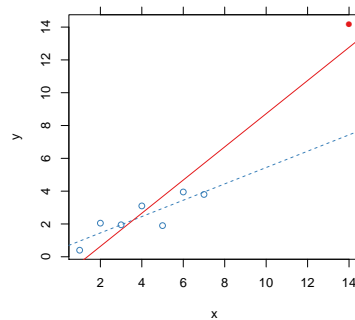
2. Each of the following scatterplots show two regression lines: the solid line is fitted to all of the points, and the dashed line is fitted to just the hollow points.



(a)



(b)



(c)

- (a) For each of the three cases, when the solid point is added to the dataset, is its residual from the least squares line large or small?

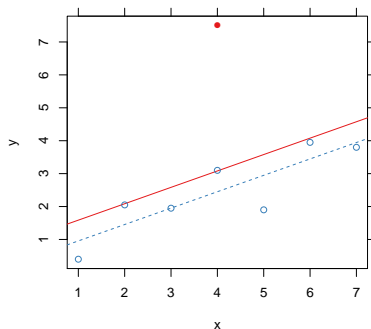
- (b) Is the  $x$  value of the solid point close to  $\bar{x}$  or far away from  $\bar{x}$ ?

- (c) What affect does adding the solid point have on  $\hat{\beta}_0$ ,  $\hat{\beta}_1$ , and  $R^2$ ?

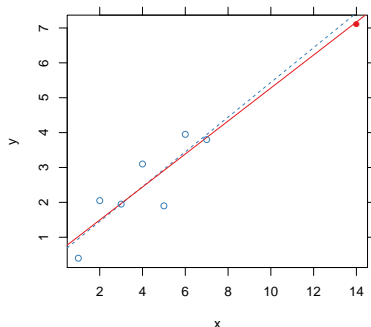
- (d) Should we include the solid point in the regression analysis? If not, what should we do with it?

## Outliers, leverage, and influence

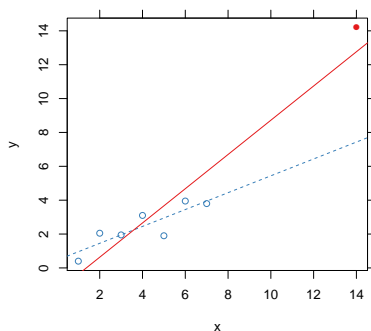
3. The following tables gives the observation number ( $i$ ), the standardized residual ( $r_i$ ), the leverage ( $h_i$ ), and Cook's distance ( $C_i$ ) for each data point. The solid point is observation 8.



Obs.	Std. Resid.	Leverage	Cook's Dist.
1	-0.78	0.45	$2 \times 10^{-1}$
2	-0.02	0.27	$7 \times 10^{-5}$
3	-0.34	0.16	$1 \times 10^{-2}$
4	0.01	0.12	$7 \times 10^{-6}$
5	-0.90	0.16	$8 \times 10^{-2}$
6	-0.07	0.27	$1 \times 10^{-3}$
7	-0.51	0.45	$1 \times 10^{-1}$
8	2.32	0.12	$4 \times 10^{-1}$



Obs.	Std. Resid.	Leverage	Cook's Dist.
1	-1.14	0.28	$3 \times 10^{-1}$
2	0.98	0.22	$1 \times 10^{-1}$
3	-0.03	0.17	$8 \times 10^{-5}$
4	1.11	0.14	$1 \times 10^{-1}$
5	-1.68	0.13	$2 \times 10^{-1}$
6	0.94	0.13	$7 \times 10^{-2}$
7	-0.10	0.15	$9 \times 10^{-4}$
8	-0.24	0.79	$1 \times 10^{-1}$



Obs.	Std. Resid.	Leverage	Cook's Dist.
1	0.64	0.28	0.081
2	1.12	0.22	0.174
3	0.24	0.17	0.006
4	0.34	0.14	0.009
5	-1.33	0.13	0.126
6	-0.55	0.13	0.022
7	-1.44	0.15	0.185
8	2.19	0.79	8.892

In each of the three cases are any of the standardized residual, leverage, or Cook's distance large for observation 8? What counts as "large" for these diagnostics?

## Summary

4. Should an outlier or a point with high leverage always be removed from a regression analysis?
5. If we decide to remove a point from an analysis, what should we do with the point?
6. Does a leverage point always have a high Cook's Distance?
7. Can a point have low leverage and high Cook's Distance?