Regression Inference and Forecasting STAT-UB.0103 – Statistics for Business Control and Regression Models

Inference

1. Here are the least squares estimates from the fit to model

$$Price = \beta_0 + \beta_1 \operatorname{Size} + \varepsilon,$$

where price is measured in units of 100 and size is measured in units of 100 ft².

The regression equation is price = 182 + 45.0 size Coef SE Coef Т Ρ 182.27 62.43 2.92 0.010 Constant 44.95 4.37 10.29 0.000 size S = 101.4R-Sq = 86.9%R-Sq(adj) = 86%

(a) Construct a 95% confidence interval for β_1 .

(b) What is the meaning of the confidence interval for β_1 ?

(c) What is the meaning of a 95% confidence interval for β_0 ? In the context of the housing data, is this useful?

(d) Perform a hypothesis test at level 5% of whether or not the is a linear relationship between Size and mean Price.

2. 44 NYU undergraduates reported the amount of time they spent communicating via email and via social media (in minutes per week). We will use this data to examine the relationship between email usage and social media usage. We fit the model

$$\text{Email} = \beta_0 + \beta_1 \text{Social} + \varepsilon.$$

using least-squares. The scatterplot and Minitab regression output follow.



The regression equation is Email = 27.8 + 0.317 Social

Predictor	Coef	SE Coef	Т	Р
Constant	27.78	19.32	1.44	0.158
Social	0.31744	0.08109	3.91	0.000

S = 81.0720 R-Sq = 26.7% R-Sq(adj) = 25.0%

Analysis of Variance

Source	DF	SS	MS	F	Р
Regression	1	100716	100716	15.32	0.000
Residual Error	42	276052	6573		
Total	43	376768			

Unusual Observations

Obs	Social	Email	Fit	SE Fit	Residual	St Resid
14	350	450.0	138.9	18.1	311.1	3.94R
16	600	300.0	218.2	35.8	81.8	1.12 X
45	280	280.0	116.7	14.5	163.3	2.05R



(a) Use the residual plots below to assess whether or not the regression assumptions hold.

(b) Is there a significant linear relationship between social media usage and email usage?

(c) Quantify the relationship between email usage and social media usage using a 95% confidence interval. (You will need the value $t_{.025} = 2.018$.)

Forecasting

3. Here are the least squares estimates from the fit to model Price = $\beta_0 + \beta_1 \operatorname{Size} + \varepsilon$, where price is measured in units of \$1000 and size is measured in units of 100 ft², along with the result of using the model to predict the mean price at size 2000 ft².

The regression equation is price = 182 + 45.0 size SE Coef Ρ Coef Т Constant 182.27 62.43 2.92 0.010 size 44.95 4.37 10.29 0.000 S = 101.4R-Sq = 86.9%R-Sq(adj) = 86%Predicted Values for New Observations NewObs Fit SE Fit 95% CI 95% PI 38.1 (1000.4, 1162.1) (851.7, 1310.9) 1 1081.3 Values of Predictors for New Observations NewObs size 20.0 1

(a) Find a 95% confidence interval for the mean price of all apartments with size 2000 ft^2 .

(b) Find a 95% prediction interval for the price of a particular apartments with size 2000 ft^2 .

(c) Make a statement about the prices of 95% of all apartments with size 2000 ft².

(d) What is the difference between the confidence interval and the prediction interval?